

Key Homework 4

$$C_{v,vib} = \sum_{j=1}^{\infty} \left[\left(\frac{\Theta_{vib,j}}{T} \right)^2 \frac{e^{-\Theta_{vib,j}/T}}{(1 - e^{-\Theta_{vib,j}/T})^2} \right] \quad \text{Eq 18.48}$$

each term of sum represents
Contribution from each normal mode

$$\Theta_{vib}^{\text{H}_2\text{O}} = \underset{\textcircled{1}}{5360 \text{ K}}, \underset{\textcircled{2}}{5160 \text{ K}}, \underset{\textcircled{3}}{2290 \text{ K}} \quad T = 600 \text{ K}$$

$$\textcircled{1} \frac{C_v}{R} = \left(\frac{5360}{600} \right)^2 \frac{e^{-5360/600}}{(1 - e^{-5360/600})^2} = 1.05 \times 10^{-2}$$

$$\textcircled{2} \quad C_v/R = 1.36 \times 10^{-2}$$

$$\textcircled{3} \quad C_v/R = 0.335 \quad \text{largest contribution... from below - this is the bending mode}$$

$$C_v/R \text{ total} = 0.359$$

NIST

Symmetric stretch 3657 cm^{-1}

bend 1595 cm^{-1}

antisymmetric stretch 3756 cm^{-1}

$$\Theta_{vib} = \frac{h\nu}{k_B} = \frac{hc\tilde{\nu}}{k_B}$$

$$\Theta_{vib} = 5267.7 \text{ K} \sim \textcircled{2}$$

$$\Theta_{vib} = 2297.5 \text{ K} \sim \textcircled{3}$$

$$\Theta_{vib} = 5410.3 \text{ K} \sim \textcircled{1}$$